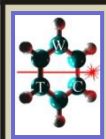


# Optical fiber interferometry

- **Signal processing**
  - **optical considerations**





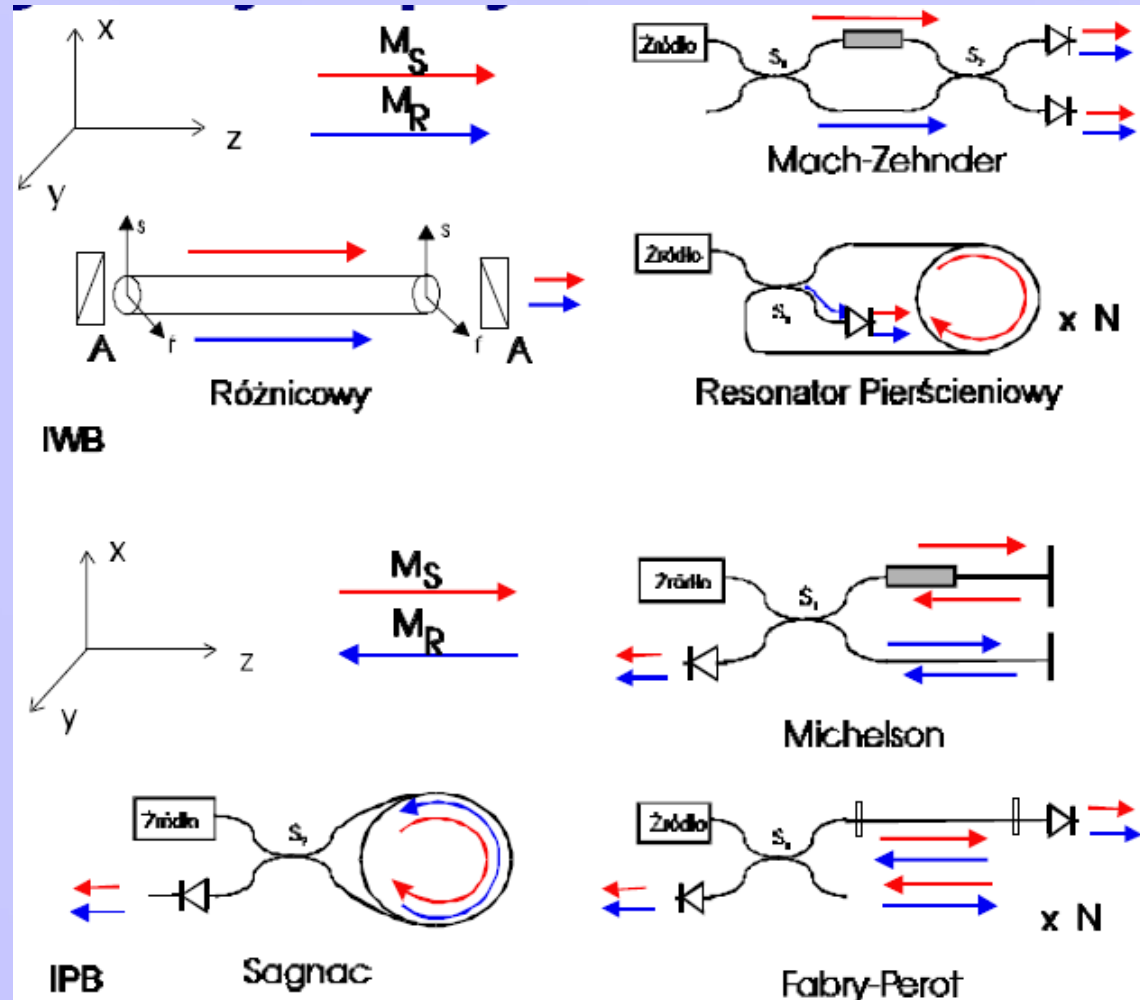
# Optical processing

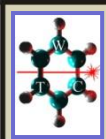
The phase or polarization demodulation optical carrier is obtained by interferometer system application, further signal processing on useful form is realized by electronics processing.

**IWB** (CMW) – Common-way interferometer  
**IPB** (CCW) – Counter-way interferometer

ANALYSE:

- 1. Coupler influence
- 2. PT localisation influence
- 3. Configuration influence





With polarisation – ideal construction: the Kapron law about an optical system equivalence:

$$\mathbf{M}_s \equiv \mathbf{R}(\Omega)\mathbf{G}(\delta)\mathbf{M}(\Phi)$$

The Jones vector for the optical source:

$$\mathbf{E} = e^{i\omega x} \begin{bmatrix} E_x \\ E_y e^{i\Delta} \end{bmatrix} = \dots = \begin{bmatrix} E_x \\ E_y e^{i\Delta} \end{bmatrix} = \dots = \begin{bmatrix} \cos \beta \\ \sin \beta e^{i\Delta} \end{bmatrix}$$

General matrix of system:

$$m = \mathbf{E}_{we}^+ \mathbf{M}_R^+ \mathbf{M}_S \mathbf{E}_{we} \in \mathbb{C}$$

Transfer function:

$$I = 0.5 \{ 1 \pm V \cos [\phi' + \phi_0] \}$$

$$V = \text{Abs}(m)$$

Scale factor

Responsitivity

$$\phi' = f(\phi)$$

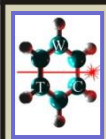
Configuration

Dynamic range

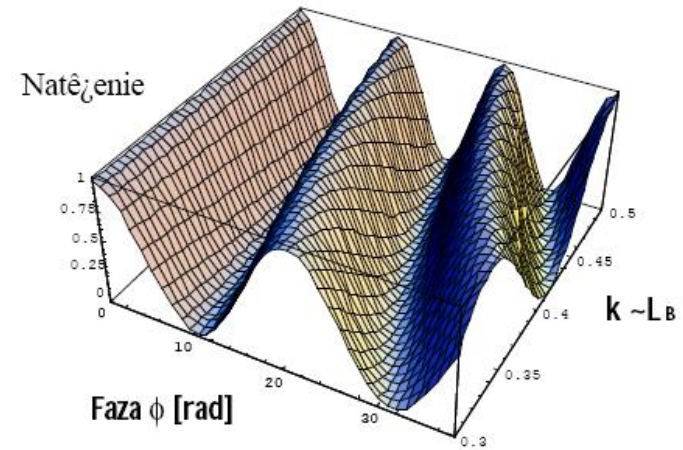
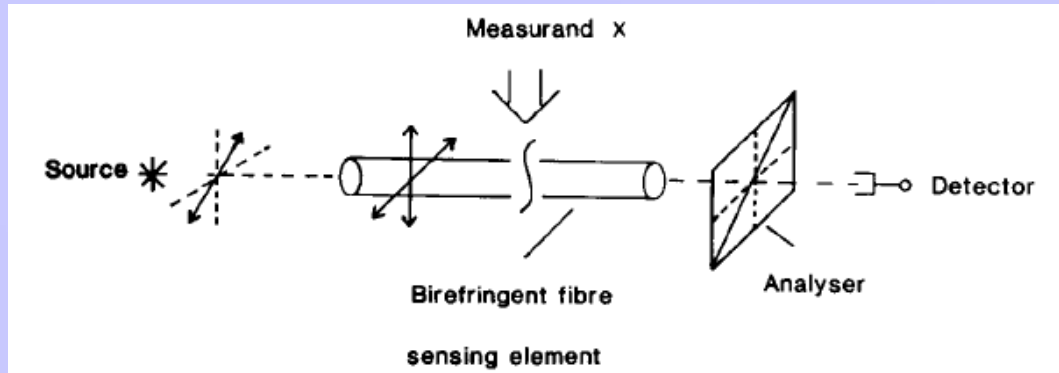
$$\phi_0 = \arg(m)$$

Bias

Drift



## Linear polarimeter:



## Transfer function:

$$\mathbf{E}_1 = \mathbf{A}(\alpha) \mathbf{F} \mathbf{E}_0$$

$$\mathbf{A} = \begin{pmatrix} \cos^2 \alpha & \sin \alpha \cos \alpha \\ \sin \alpha \cos \alpha & \sin^2 \alpha \end{pmatrix}$$

$$\mathbf{F} = \begin{pmatrix} e^{i(\phi_1 + 1/2\phi_2)} & 0 \\ 0 & e^{i(\phi_1 - 1/2\phi_2)} \end{pmatrix}$$

$$\mathbf{E}_0 = \begin{pmatrix} \cos \delta \\ e^{i\beta} \sin \delta \end{pmatrix}$$

$$I = \frac{1}{2} I_0 (1 + \cos 2\alpha \cos 2\delta) [1 + V \cos(\phi_2 - \beta)]$$

for  $\delta = \alpha = \pi/4$

$$I_1 = \frac{1}{2} I_0 [1 + \cos(\phi_2 - \beta)]$$

$$V = \sin 2\alpha \sin 2\delta / (1 + \cos 2\alpha \cos 2\delta)$$

The polarisation properties change has influence only on dynamic range

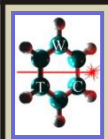
## Circular polarimeter:

$$\mathbf{F} = \begin{pmatrix} \cos \phi_3 & \sin \phi_3 \\ -\sin \phi_3 & \cos \phi_3 \end{pmatrix}$$

$$\mathbf{E}_0 = \begin{bmatrix} \cos \delta \\ \sin \delta \end{bmatrix}$$



$$I_1 = \frac{1}{2} I_0 [1 + \cos 2(\phi_3 + \delta - \alpha)]$$



**Mach-Zehnder interferometer:**

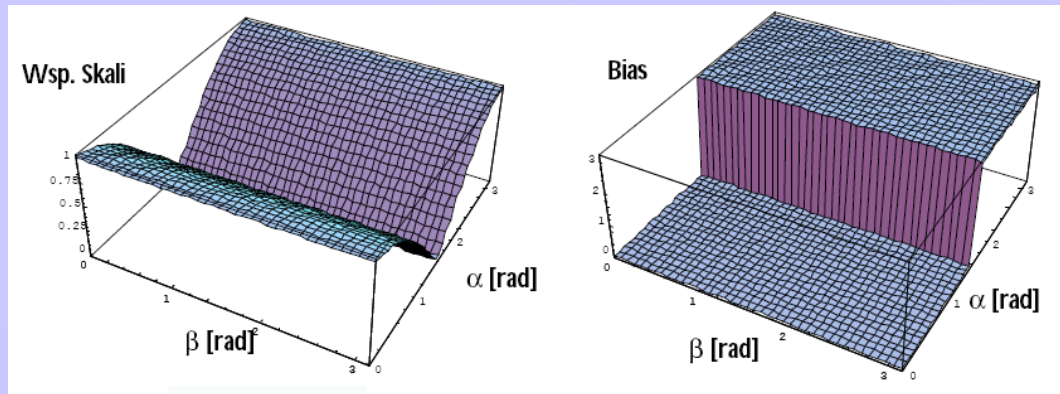
$$m = E_{wz}^+ R(\Omega) G(\delta) R(\Phi) E_{wz}$$

a. Only twist:

$$M_S = R(\alpha)$$

$$V = \sqrt{\cos^2 \alpha + \sin^2 \alpha \sin^2 (2\beta) \sin^2 \Delta}$$

$$\phi_0 = \arctg[-tg \alpha \sin (2\beta) \sin \Delta]$$

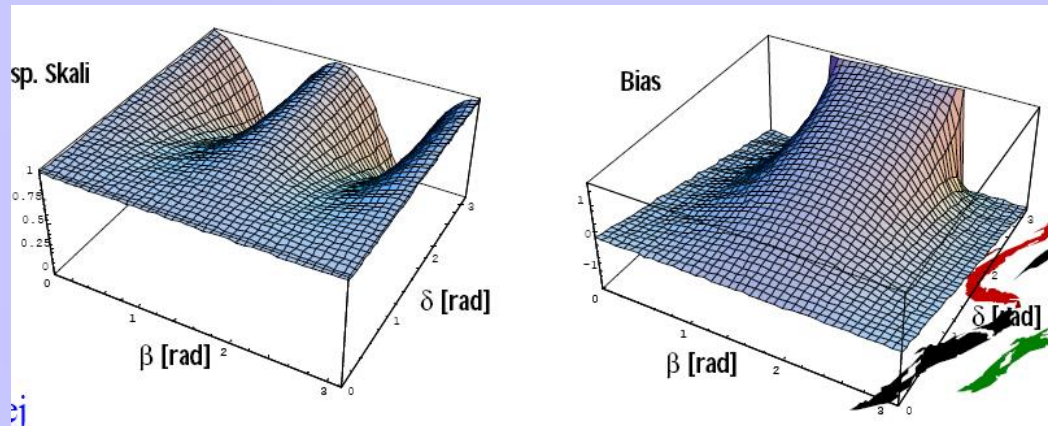


b. Only birefringence:

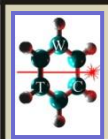
$$M_S = G(\delta)$$

$$V = \sqrt{\cos^2 (\delta/2) + \sin^2 (\delta/2) \cos (2\beta)}$$

$$\phi_0 = \arctg[-tg (\delta/2) \cos (2\beta)]$$



MZ (Ring Interferometer) is very sensitive on input SOP changes as well as polarisation properties of the optical fiber

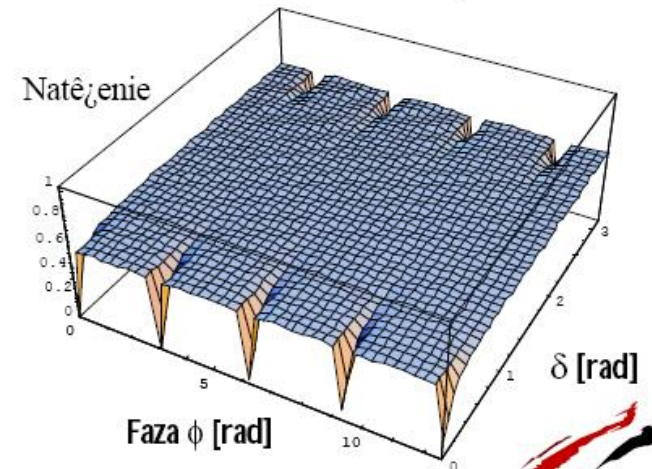
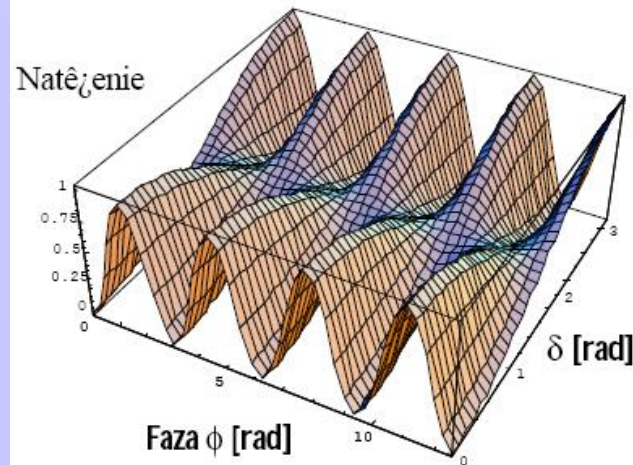
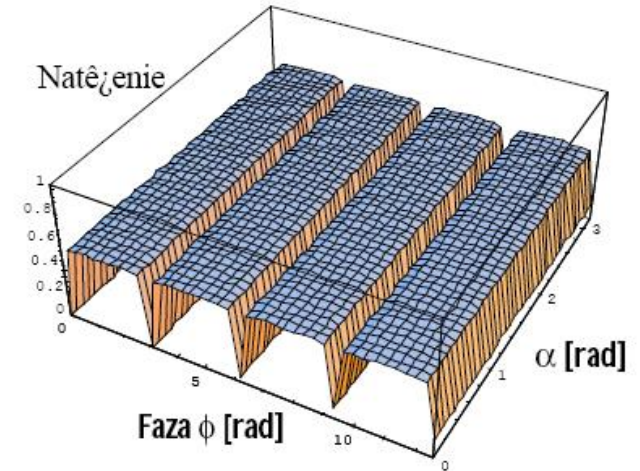
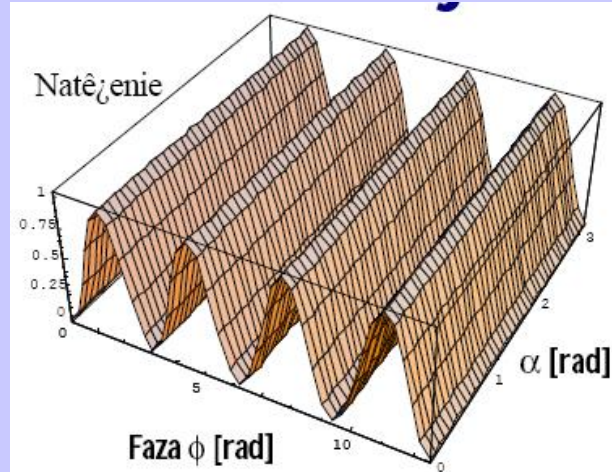


## Michelson (Fabry-Perot) interferometer:

Input beam with linear SOP  
( $\beta = \pi/4$ )

$$I = \frac{I_0}{1 + F \sin^2 \phi / 2}$$

$$F = 4R / (1 - R)^2$$

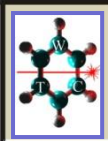


Michelson

Fabry-Perot

IM (FP) is more polarisation stabile.

Noninfluence of fiber twist, but twice bigger influence of fiber birefringence.



Sagnac interferometer:

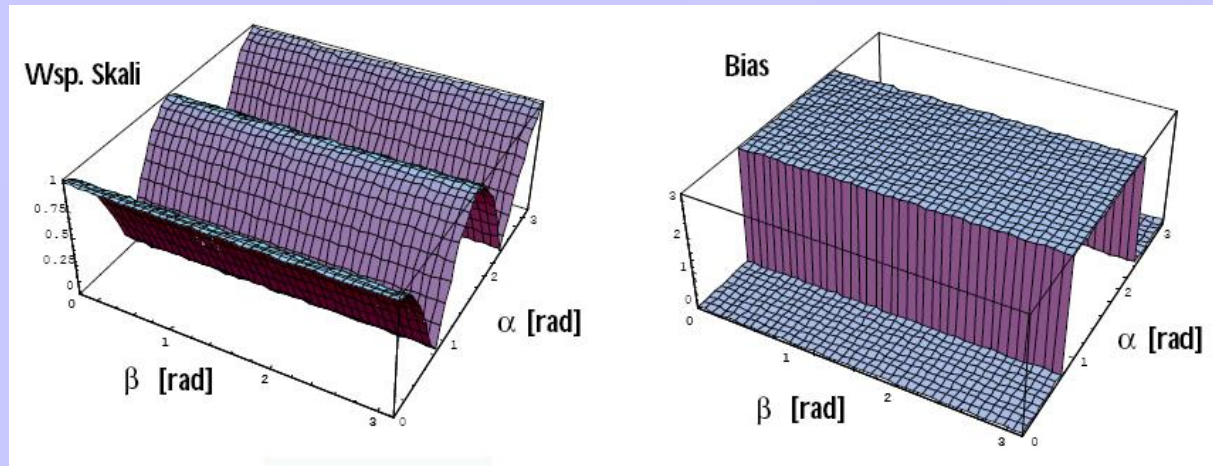
$$m = E_{wg}^+ R(\Omega) G(-\delta) R(\Phi + \Omega) G(\delta) R(\Phi) E_{wg}$$

a. Only twist:

$$M_S = R(\alpha)$$

$$V = \sqrt{\cos^2(2\alpha) + \sin^2(2\alpha)\sin^2(2\beta)\sin^2\Delta}$$

$$\phi_0 = \text{arctg}[-\text{tg}(2\alpha)\sin(2\beta)\sin\Delta]$$

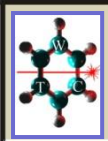


b. Only birefringence:

$$M_S = G(\delta)$$

$$V = 1 \quad \phi_0 = 0$$

The Sagnac interferometer has nonsensitivity on clear birefringence of the optical fiber.



The polarisation influence reduction:

- application Hi-BI fiber (increase system cost 3 USD/m, the elements should be adjusted according SOP)
- polarisation correction via polarization controller
- reduction of the „freedom degrees” ( $\Phi$ - $\delta$ - $\Omega$ ):
  - differential – polarisation filtration (has been shown)
  - MZ and RR unstable – active polarisation controller
  - choose the proper configuration:
    - CCW insted of CMW (more stabile)
    - SOP detection in real time (polarise-phase detection scheme)
    - reciprocal configuration of Sagnac interferometer

